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For theories T containing a sufficiently rich part of true arithmetic we characterize $T + Con_T$, where the sentence Con_T claims the consistency of T , as the minimal extension proving for some algorithm that it decides a given problem Q_0 outside PTIME as fast as any algorithm B with the property that T proves that B decides Q_0 . Moreover, we characterize problems with an optimal algorithm in terms of arithmetical theories.